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PRIOR AFFINITY MEASURES ON MATCHES FOR ICP-LIKE NONLINEAR REGISTRATION OF FREE-FORM SURFACES

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ABSTRACT

In this paper, we show that several well-known nonlinear surface registration algorithms can be put in an ICP-like framework, and thus boil down to the successive estimation of point-to-point correspondences and of a transformation between the two surfaces. We propose to enrich the ICP-like criterion with additional constraints and show that it is possible to minimise it in the same way as the original formulation, with only minor modifications in the update formulas and the same convergence properties. These constraints help the algorithm to converge to a more realistic solution and can be encoded in an affinity term between the points of the surfaces to register. This term is able to encode both a priori knowledge and higher order geometrical information in a unified manner. We illustrate the high added value of this new term on synthetic and real data.

Index Terms— registration, mesh, surface, geometrical invariants, optimisation

1. INTRODUCTION

Nonlinear registration is a key tool in medical image analysis for the understanding of anatomy in normal and pathological conditions. It allows the quantitative comparison of structures in different subjects and more generally the fusion of inter-subject data for further statistical analysis. Surfaces represented by point clouds or meshes are especially convenient to represent a subject's anatomy. In particular, they allow to isolate a specific structure or organ from the rest of the body (*eg* after segmentation from MRI data), and thus to help answer given research questions in a very specific manner. A convenient way to perform nonlinear registration of surfaces is to formulate it as a minimisation problem. Such an approach poses some specific problems, most notably the difficulty 1) to devise a criterion allowing to obtain an adequate solution (*eg* with a good compromise between regularity and closeness to the data); 2) to minimise such a criterion efficiently (*eg* with a simple scheme and proofs of convergence).

In this paper, our contributions are twofold. First, we show that several well-known nonlinear registration algorithms can actually be put in an ICP-like framework, that consists in the successive estimation of the point-to-point correspondences and the transformation between the surfaces. Such a framework yields a simple scheme with iterative update formulas for both unknowns that converges to a minimum of a well-grounded criterion (Section 2). Second, we show that it is possible to enrich this criterion with additional constraints, to make it robust using a threshold function, and to minimise it efficiently with only minor modifications in the update formulas and the same convergence properties as the original algorithm (Section 3).

These constraints help the algorithm to converge to a more realistic solution and can be encoded in an *affinity* term in the ICP-like general criterion. This affinity term is computed between the points of the two surfaces to register and comes in addition to the *proximity* term between their spatial coordinates. It is able to encode both a priori knowledge (*eg* labels of gyri/sulci for cortical registration) (Section 4.2) and higher order geometrical information (*eg* consistency between the curvatures of points to be matched) (Section 4.1) and thus handles both types of constraints in a unified manner. Finally, we evaluate the added value of this new affinity term on synthetic and real data in Section 5.

2. NON RIGID REGISTRATION AS AN ICP ALGORITHM

Numerous algorithms have been proposed for nonlinear registration of 3D surfaces [1]. Many such methods have been largely inspired by the ICP algorithm [2] whose key idea is to consider the registration problem as the interleaved estimation of point-to-point correspondences and (rigid-body) transformation between the two surfaces. In case of the ICP algorithm, this dual view is extremely useful as it allows 1) the formulation of the problem as a minimisation of a well-defined criterion; 2) the optimisation of this criterion via iterative and tractable minimisations over the correspondences and the transformation in turn; 3) a proof of convergence towards a (at least local) minimum of this criterion. In fact, these key properties can be kept for nonlinear problems using the same dual view by defining the optimal transformation between two surfaces X and Y as:

$$\tilde{T} = \arg \min_{A, T} \sum_{x_i \in X} \sum_{y_j \in Y} A_{i,j} \|y_j - T(x_i)\|^2 + \alpha L(T) \quad (1)$$

$$+ \gamma \sum_i \sum_j A_{i,j} \log(A_{i,j}) \text{ with } \forall i, \sum_j A_{i,j} = 1 \text{ and } \forall (i, j), A_{i,j} \geq 0$$

and where:

- T is the transformation best superposing the two sets of points (and that can be rigid, affine, elastic, *etc*).
- A is a $\text{card}(X) \times \text{card}(Y)$ matrix. The greater $A_{i,j}$, the more likely the point $x_i \in X$ to be the correspondent of the point $y_j \in Y$. A can be viewed as a hidden variable of the registration problem and will be called the match matrix.
- L is a regulariser allowing to penalise discontinuities of T over the space with $\alpha > 0$ weighing its influence.
- $\gamma \sum_i \sum_j A_{i,j} \log(A_{i,j})$ is a barrier function allowing to control the fuzziness of A (the higher γ , the greater the fuzziness). In practice, this term convexifies the criterion.

The key remark is that this criterion can be minimised by successive optimisation over A with T fixed and over T with A fixed:

- Step 0:** Initialise \tilde{T}
- Step 1:** $\tilde{A} = \arg \min_A \sum_{x_i \in X} \sum_{y_j \in Y} A_{i,j} \|y_j - \tilde{T}(x_i)\|^2 + \gamma \sum_i \sum_j A_{i,j} \log(A_{i,j})$ with $\sum_j A_{i,j} = 1$
- Step 2:** $\tilde{T} = \arg \min_T \sum_{x_i \in X} \sum_{y_j \in Y} \tilde{A}_{i,j} \|y_j - T(x_i)\|^2 + \alpha L(T)$
- Step 3:** if \tilde{T} has changed go to Step 1 else exit

This iterative scheme is simple and ensures a monotonical decrease of the criterion (for any transformation T and regulariser L) and thus a convergence towards a (at least) local minimum. Note that the fuzziness of A and the regularity of T can be adapted throughout the iterations by varying (typically decreasing) the parameters α and γ .

The main challenge is then to define proper T and L to make Steps 1 and 2 tractable. Below we list several algorithms fitting in this general ICP-like formulation and detail their choices to do so:

▷ The original ICP algorithm [2] where T is a rigid-body transformation, L is the null function and γ is equal to zero. Step 1 is solved setting $A_{i,j}$ to one if and only y_j is the closest point of $T(x_i)$ in Y and zero else (typically using a *kd-tree*). Solving Step 2 then consists in finding the transformation that best superposes the correspondences established during Step 1 in the least squares sense.

▷ The TPS-RPM algorithm [3] where T and L encode smoothing Thin Plate Splines and γ is typically set to decrease from infinity (maximal fuzziness) to zero (no fuzziness *i.e.* A is binary) throughout the iterations. Steps 1 and 2 have a simple closed-form solution but Step 2 requires the inversion of a matrix of size proportional to $\text{card}(X) \times \text{card}(Y)$ which limits the application of this approach to small data sets (typically of size lower than about 1000 points).

▷ The locally affine algorithm [4] where T is decomposed into several local affine transformations. Thus, an affine transformation T_k is assigned to each point x_k of the mesh X and spatial coherency is ensured by a regularisation on the T_k s over the space:

$$L(T) = (T_k)_{k=1, \dots, \text{card}(X)} = \sum_{(k1, k2) \in C_2} \|T_{k1} - T_{k2}\|_F^2$$

where $\|\cdot\|_F$ is the Frobenius norm and C_2 the set containing the indices of points of X that are neighbours. The parameter γ is set to zero (thus Step 1 is solved in the same way as the original ICP). Step 2 is solved by the successive minimisation over the T_k s in turn, using a Markovian interpretation. This implementation allows a fast registration on huge data (about 3 min for a surface of 100K points).

3. A NEW TERM IN THE CRITERION

3.1. A priori affinity function

The computation of A is essentially based on the spatial proximity between the points $T(x_i)$ and y_j , which is a bad indicator of whether x_i and y_j should be matched or not, especially at the beginning of the iterative scheme, when the two surfaces are likely to be far from each other. Some previous efforts have been made to include richer information in the matching process in addition to the *spatial proximity* term $\|y_j - T(x_i)\|$, *eg* based on the similarity of the normals at points $T(x_i)$ and y_j [5]. Unfortunately, such approaches make Step 2 intractable because, in essence, when T is non-rigid, the normal at $T(x_i)$ does not only depend on T and on the normal at x_i , but also on the neighbours of $T(x_i)$. We suggest an alternative approach, where we propose to add an *affinity* term between the points to be matched, that is independent of 1) the spatial proximity between the points of the two surfaces and 2) the unknown transformation T . Actually,

this affinity term gives a very general and convenient framework to include heterogeneous sources of a priori knowledge in the registration process. It is equally able to encode simple ideas such as "two points with similar curvatures are more likely to be matched than others" as well as knowledge of the labels of structures in the objects to be matched (*eg* gyri/sulci in cortical registration). The key property of this affinity term is that it allows both steps of the algorithm to remain tractable, while limiting the influence of local minima and speeding up the overall iterative scheme. The resulting algorithm shares similar convergence properties with the original one.

Thus, in order to encode the affinity between points of X and Y , we introduce an affinity cost function $c : X \times Y \rightarrow \mathbb{R}^+$ such that the more similar (in a sense to be defined) x and y , the closer to zero $c(x, y)$. Then we rewrite the general criterion 1 as:

$$\tilde{T} = \arg \min_{A, T} \sum_{x_i \in X} \sum_{y_j \in Y} A_{i,j} [\|y_j - T(x_i)\|^2 + \beta c(x_i, y_j)] + \alpha L(T) + \gamma \sum_i \sum_j A_{i,j} \log(A_{i,j}) \text{ with } \forall i, \sum_j A_{i,j} = 1 \quad (2)$$

where β is a positive parameter weighting the influence of c .

As the function c does not depend on T , adding the affinity cost function c only affects Step 1 of the algorithm which becomes:

$$\tilde{A} = \arg \min_A \sum_{x_i \in X} \sum_{y_j \in Y} A_{i,j} [\|y_j - T(x_i)\|^2 + \beta c(x_i, y_j)] + \gamma \sum_i \sum_j A_{i,j} \log(A_{i,j}) \text{ with } \forall i, \sum_j A_{i,j} = 1.$$

This step is solved by:

$$\begin{cases} \text{for all } (i, j); A_{i,j} = \exp(-(\|y_j - T(x_i)\|^2 + \beta c(x_i, y_j))/\gamma) \\ \text{normalise each row of } A \end{cases}$$

3.2. Fast and robust implementation

This algorithm to solve Step 1 has the same time and space complexity as in the TPS-RPM algorithm, that is $\mathcal{O}(\text{card}(X) \times \text{card}(Y))$. To reduce this complexity, we propose to modify the original criterion by introducing a threshold function $\rho_\delta : x \mapsto x$ if $x < \delta$ and δ else (with $\delta > 0$). The criterion then becomes:

$$\tilde{T} = \arg \min_{A, T} \sum_{x_i \in X} \sum_{y_j \in Y} A_{i,j} \rho_\delta(\|y_j - T(x_i)\|^2 + \beta c(x_i, y_j)) + \alpha L(T) + \gamma \sum_i \sum_j A_{i,j} \log(A_{i,j}) \text{ with } \forall i, \sum_j A_{i,j} = 1 \quad (3)$$

This function ρ_δ allows to consider as outliers the points of X for which there do not exist points of Y such that $\|y_j - T(x_i)\|^2 + \beta \times c(x_i, y_j) < \delta$. It allows to make A sparse (which reduces the space complexity) and to use a *kd-tree* (which reduces the time complexity to $\mathcal{O}(\text{card}(X) \times \log(\text{card}(Y)))$). This way, the overall minimisation scheme becomes both more robust and more efficient:

Step 1:

initialise A to the null matrix

for all $x_i \in X$;

$S = \{y_j \in Y \text{ such that } \|y_j - \tilde{T}(x_i)\|^2 < \delta\}$ (using a *kd-tree*)

• if $\exists y_j \in S$ such that $\|y_j - \tilde{T}(x_i)\|^2 + \beta c(x_i, y_j) \leq \delta$

▷ if $\gamma \neq 0$ (A is fuzzy)

for all $y_j \in S$ such that $\|y_j - \tilde{T}(x_i)\|^2 + \beta c(x_i, y_j) \leq \delta$

$\tilde{A}_{i,j} = \exp(-(\|y_j - \tilde{T}(x_i)\|^2 + \beta c(x_i, y_j))/\gamma)$

normalise the i^{th} row of A

▷ else (asymptotical case where A is binary)

$\tilde{A}_{i,j} = 1$ for $y_j = \arg \min_{y \in S} \|y - \tilde{T}(x_i)\|^2 + \beta c(x_i, y)$

• else consider x_i as an outlier

Step 2:

$\tilde{T} = \arg \min_T \sum_{x_i \in X} \sum_{y_j \in Y} \tilde{A}_{i,j} \|y_j - T(x_i)\|^2 + \alpha L(T)$

Step 3: if \tilde{T} has changed go to Step 1 else exit

One can see that the i^{th} line of A is left equal to zero in case x_i is an outlier, which allows A to be sparse. This seems to break the constraint $\sum_j A_{i,j} = 1$. Actually, it can be shown that this simpler scheme gives the same solution as the complete and more involved one that consists in, for each outlier x_i , and each y_j , setting $\tilde{A}_{i,j} = 1/\text{card}(Y)$ in Step 1 and replacing $\|y_j - T(x_i)\|$ by δ in Step 2. Moreover, note that to reduce the complexity further, one can either i) consider only the $\tilde{A}_{i,j}$ s with the highest values $\forall i$ or ii) approximate $\sum_{x_i \in X} \sum_{y_j \in Y} \tilde{A}_{i,j} \|y_j - T(x_i)\|^2$ by $\sum_{x_i \in X} \|y_i^G - T(x_i)\|^2$ with $y_i^G = \sum_j \tilde{A}_{i,j} y_j \forall i$ during Step 2.

3.3. Implementation details

3.3.1. Choice for β , α , γ , δ

The parameter β weighs the influence of the affinity term wrt the spatial proximity term. Intuitively, if $\beta \rightarrow \infty$, only the prior knowledge will be used to build matrix A . Reciprocally, if $\beta \rightarrow 0$, the criterion becomes the one defined by Eq 1. In practice, we first give β a high value to guide the registration by the a priori affinity function when the surfaces are distant to each other and then to reduce this value throughout the iterations to reduce its influence (and in particular potential ambiguities/errors in the computation of affinities). Quite similar interpretations on how the other parameters influence the solution can be made concerning α (regularisation), γ (fuzziness) and δ (robustness). Thus we typically initialise these parameters with high values and reduce them throughout the iterations.

3.3.2. Initialisation

As the original ICP, this nonlinear registration algorithm needs a proper initialisation (Step 0) to converge to an appropriate solution. A classical method for this purpose is the alignment of the two surfaces based on their principal axes and centres of mass. This is usually inadequate, as these quantities are the output of a least squares minimisation over all the points of the meshes, and thus likely to be very different in case of very dissimilar surfaces. For instance, this can be the case when X is a subset of Y (or the contrary). The use of the affinity cost function allows to alleviate this problem as follows. We keep the pairs (x, y) with a high affinity (that is, $c(x, y)$ has a value lower than a predefined threshold value τ) and we use these selected pairs to compute an affine transformation and initialise the nonlinear registration via a RANSAC procedure [6] (with the additional constraint of one-to-one matches between the two surfaces, which prevents the optimal solution from being a degenerate matrix).

4. THE A PRIORI AFFINITY FUNCTION C

The a priori affinity functions c can either be based on local geometrical features (Section 4.1) or on predefined labels (Section 4.2).

4.1. Local geometry based affinity function

This approach is based on i) extracting distinctive keypoints on both surfaces X and Y , ii) building a local surface descriptor for each keypoint and iii) building a cost function c for each pair of points (x, y) (that can either be keypoints or non-keypoints). Both keypoints and local surface descriptors are chosen to be as invariant as possible to the unknown nonlinear transformation T , and thus so is the resulting cost function c , as specified earlier.

i) *Detecting keypoints.* The *crest lines* are curves on the surface along which the surface bends sharply. They constitute strong and robust anatomical features and thus are formed by relevant interest points. We simply define these lines as minimum spanning sub-graphs of a neighbour graph (in which each edge connecting two points is given a weight depending on the curvature at these points) [7].

ii) *Choosing an adequate descriptor.* Most classical local surface descriptors have been devised for pose estimation and are only invariant to isometries [8, 9]. To the best of our knowledge, there exists no efficient descriptor invariant to any nonlinear or even affine transformation. The shape index [10] is a local shape descriptor invariant to similarities and is easy to compute as it only depends on the principal curvatures. Thus it constitutes a useful local descriptor:

$$s(x) = \frac{2}{\pi} \arctan\left(\frac{k1(x)+k2(x)}{k1(x)-k2(x)}\right)$$

where $k1(x)$ and $k2(x)$ are the min and max curvature values at x .

iii) *Computing the affinity between points.* The affinity measure $c(x, y)$ between two keypoints x and y is based on the comparison of their descriptors $s(x)$ and $s(y)$. However, it is necessary to include non keypoints to build c . Thus, we choose to design c as $c(x, y) = \min(|s(x) - s(y)|_{L1}, l)$ if x and y are keypoints and $c(x, y) = l$ else. The l variable is very important because it determines the ability of a keypoint to be matched to a non keypoint. This way, during Step 1, for a keypoint x_i , if there exists no keypoint y of Y such that $c(x, y) \leq l$, only the spatial proximity term will be used to build line i of matrix A . In practice, we empirically choose to set $l = c_{max}/2$, where c_{max} is the maximum value that can take $|s(x) - s(y)|_{L1}$ when x and y are keypoints.

4.2. Labellisation based affinity function

Another approach consists in affecting labels to points of X and Y (eg brain sulci/gyri). This way, the affinity function consists in establishing a set of n disjoint labels and designing c as $c(x, y) = 0$ if x and y have the same label and $c(x, y) = p$ else.

5. EXPERIMENTS & RESULTS

In the following, we use a locally affine model for the transformation [4] (because of its ability to perform efficiently on large data sets) and we evaluate the impact of using $(\gamma, \beta \neq 0)$ and not using $(\gamma, \beta = 0)$ the fuzziness and affinity terms on the accuracy and robustness of the algorithm. When using these two terms, γ and β are updated every 10 iterations of the overall scheme (Section 3.2), and so are α and δ . The update formulas are: α for the additive component of the affine transformation: $\alpha_{init}^t = 200$ is divided by 1.1 until α^t reaches 0.5; α for the multiplicative component: $\alpha_{init}^m = 700$; β : $\beta_{init} = 25$ is divided by 1.4 until β reaches 0.001; δ : $\delta_{init} = 400$ is divided by 1.2 until δ reaches 25; γ : $\gamma_{init} = 20$ is divided by 1.2 until γ reaches 0.05. Moreover, we consider as more reliable the matches coming from keypoints or labelled points, and thus we give them more importance in the estimation of T in Step 2.

5.1. Experiments on synthetic data

Generation of ground truth data. We first segment a structure X (typically, a pair of lateral ventricles or caudate nuclei, giving surfaces of about 10,000 points, itknap.org) from a 3T T1-weighted brain MRI of a healthy subject. Then Y is generated from X by applying a random thin plate spline transformation. To simulate such a transformation, we select a set of 8 landmarks on X and randomly move them independently in a sphere of radius 20 mm around their initial position. Then, we add a uniform Gaussian noise of std 0.5 mm on each point of the deformed surface and remove groups of adjacent vertices to generate holes. This way we generate ground truth pairs of 10 ventricles and 10 caudate nuclei. Note that we deliberately choose to apply a transformation coming from a model different from that assumed by our algorithm.

Evaluation. We evaluate the registration error by computing the mean distance between homologous points after registration. The results are reported in Table 1 and an example is displayed in Figure

1. On both anatomical structures, the added value of using fuzziness alone ($\gamma \neq 0, \beta = 0$) is about 35% and of using both fuzziness and affinity ($\gamma, \beta \neq 0$) is about 52% compared to using none ($\gamma, \beta = 0$).

	$\gamma, \beta = 0$	$\gamma \neq 0, \beta = 0$	$\gamma, \beta \neq 0$
caudate nuclei	1.64 ± 1.32	1.12 ± 0.86	0.78 ± 0.63
ventricles	2.45 ± 1.40	1.46 ± 1.05	1.17 ± 0.93

Table 1. Experiments on synthetic data (stats). Mean and std (mm) of the registration error for the 10 ventricles and 10 caudate nuclei by varying the fuzziness and affinity parameters.

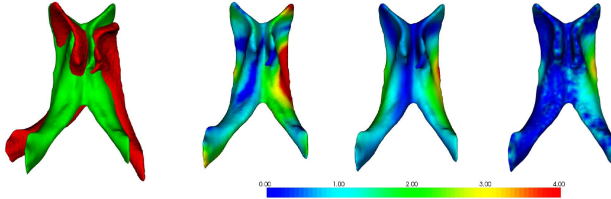


Fig. 1. Experiments on synthetic data. From left to right: 1) original (green) and deformed (red) ventricles; 2) mapping of registration error with $\gamma, \beta = 0$ (no fuzziness, no affinity); 3) $\gamma \neq 0, \beta = 0$, (fuzziness, no affinity); 4) $\gamma, \beta \neq 0$ (fuzziness, affinity).

5.2. Results on real data

In the following, we always use the fuzziness term ($\gamma \neq 0$). In a first experiment, we evaluate qualitatively the added value of the affinity term i) to map asymmetries [11] of caudate nuclei (whose asymmetries have been related to attention-deficit disorders in children) (Fig 2) and ii) on the registration of the horns of lateral ventricles (Fig 3). We observe that the impact of using the affinity term is especially prominent in areas where crest lines have been detected. In a second experiment, we segment the brain from T1-weighted MRI data of two healthy subjects (300,000 points, `brainvisa.info`), and we extract four sulcal fundus beds automatically (using our algorithm for crest lines) and label them manually for each subject. Then we register the two surfaces i) without using any a priori knowledge ($\beta = 0$) and ii) using only 3 out of the 4 sulcal fundus beds to compute the affinity function ($\beta \neq 0$) (Sec 4.2). The error on the fourth sulcus is used as a quality metric of the registration. It is evaluated to be 7 mm in the first case ($\beta = 0$) and 3 mm in the second ($\beta \neq 0$). This suggests the usefulness of the affinity term (Fig 4).

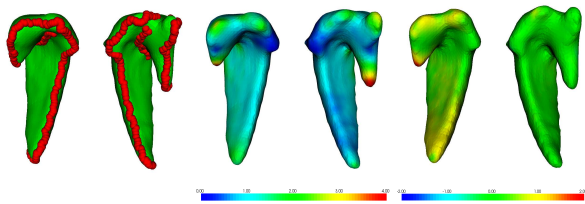


Fig. 2. Experiments on real data (caudate nuclei). From left to right: 1) crest lines; 2) asymmetry map without using the affinity term ($\beta = 0$); 3) added value of using the affinity term ($\beta \neq 0$).

6. CONCLUSION & PERSPECTIVES

We introduced an a priori affinity term in an ICP-like criterion for nonlinear registration of surfaces. We then derived a robust and

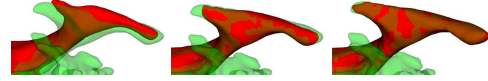


Fig. 3. Experiments on real data (inferior and posterior horn of the ventricles). From left to right: initial view of the two surfaces, registration without ($\beta = 0$) and with ($\beta \neq 0$) the affinity term. Note that the badly segmented third ventricle in one of the surfaces (green) does not influence negatively the registration result.

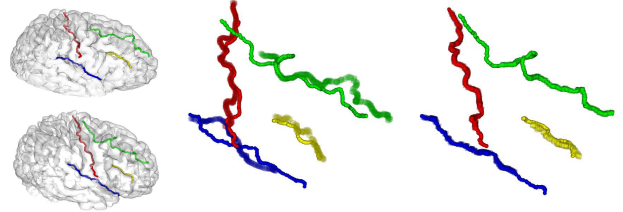


Fig. 4. Experiments on real data (brain). The four sulci are the central (red), lateral (blue), superior frontal (green) and inferior frontal (yellow) sulci. From left to right: 1) brain 1 (top) and brain 2 (bottom); 2) brain 2 (with sulci shown in transparency) towards brain 1 without using the affinity term; 3) brain 2 towards brain 1 using the constraints on three of the sulci via the affinity term. The fourth - inferior frontal (yellow) - sulcus is better registered using the three others as a constraint.

convergent scheme to minimise this criterion and showed the added value of the new term for registration of various brain structures. The overall algorithm is modular, and other implementation choices could be tested. In particular, the affinity term could be built using other descriptors (with the goal to achieve invariance to affine or more general nonlinear transformations rather than just similarities) or based on probabilistic atlases when available (*eg* for gyri or sulci) and could be extended to all points instead of only salient points. Moreover, it could be interesting to preserve the line structure of salient lines during the matching process of their points (Step 1).

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